

Algebra 1 Final Exam Review

Name KEY

1) Determine the factored form of the following quadratic functions.

a. $x^2 - 14x - 15$

b. $3x^2 + 12x - 36$

$(x-15)(x+1)$ $3(x^2+4x-12) = 3(x+6)(x-2)$

2) Determine the solutions to the following quadratic functions.

a. $3x^2 = 27$

b. $2x^2 - 3 = -4x$

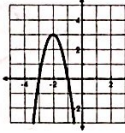
$x^2 = 9$ $x = \pm 3$ $2x^2 + 4x - 3 = 0$

$\frac{-4 \pm \sqrt{4^2 - 4(2)(-3)}}{2(2)}$

3) Use the graph to the right to answer the questions.

a. Determine the vertex.

$(-2, 3)$
 $(-\infty, -2)$
 $(-2, \infty)$



b. Determine the increasing interval.

c. Determine the decreasing interval.

$\frac{\pm \sqrt{10-2}}{2}$

4) Write the quadratic equation of the graph of the parent function, $y = x^2$, that has been shifted down 3 units and stretched by a factor of 2.

$y = 2(x-0)^2 - 3$

Remember All shifts from vertex form: $y = a(x-h)^2 + k$

a: stretch/shrink (-) reflect vertex: $(-h, k)$
h: left/right x-axis Axis of Symmetry: $y = -h$
k: up/down

5) An object is projected into the air with a path described by the function $h(t) = -16t^2 + 96t + 160$ where h is the height above the ground in feet and t is the time in seconds since the object started along the path.

a. Find the time the object changes direction.

b. Find the maximum height of the object.

$-b/2a = -96/2(-16) = 3$

$-16(3)^2 + 96(3) + 160 = 304$

c. Describe the location of the object at 2.5 seconds.

d. Describe the location of the object at 4.1 secs.

going up

going down

6) When a quadratic expression consists of two perfect square terms which are being subtracted, then this quadratic can be factored using the DOTS method.

7) Completing the Square is a method for solving Quadratics.

8) Quadratic functions whose graphs open up have local minima.

9) The vertex of a quadratic function always lies on the axis of symmetry.

10) Write down examples of functions for each of the following:

a. linear increase

b. exponential growth

c. linear decrease

d. exponential decay

$y = 2x$ $y = (2)^x$ $y = -2x$ $y = (1/2)^x$

11) For each table, write the best description, then write the appropriate function.

a.

x	0	1	2	3	4
f(x)	27	9	3	1	1/3

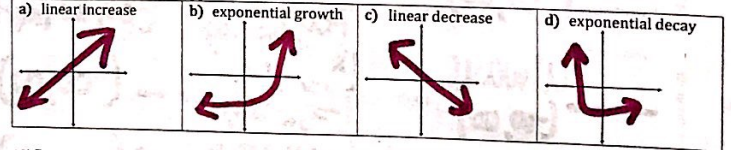
description: exponential
function: $y = 27(1/3)^x$

b.

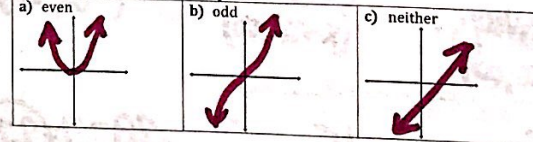
x	0	1	2	3	4
f(x)	3	0	-1	0	3

description: Quadratic
function: $y = x^2$

12) Sketch a graph for each type of function.



13) Draw a graph for each description.



14) Write examples of functions for each description.







a) even $y = 2$ b) odd $y = 2x$ c) neither $y = 2x + 6$

15) Determine the equation for the following situation: Becky began with 4 bugs. She noticed that they increased by a factor of 1.5 every year.

$4(1.5)^x$

16) When comparing linear growth and exponential growth, the exponential function will always eventually win.

17) Sketch an example of each type of function & then identify each characteristic.

	Linear:	Quadratic:	Exponential:
PICTURE	Increase:  Decrease: 	Opens Up:  Opens Down: 	Growth:  Decay: 
END BEHAVIOR	Increase: As $x \rightarrow -\infty, y \rightarrow -\infty$ As $x \rightarrow \infty, y \rightarrow \infty$ Decrease: As $x \rightarrow -\infty, y \rightarrow \infty$ As $x \rightarrow \infty, y \rightarrow -\infty$	Opens Up: As $x \rightarrow -\infty, y \rightarrow \infty$ As $x \rightarrow \infty, y \rightarrow \infty$ Opens Down: As $x \rightarrow -\infty, y \rightarrow -\infty$ As $x \rightarrow \infty, y \rightarrow -\infty$	Growth: As $x \rightarrow -\infty, y \rightarrow$ asymptote As $x \rightarrow \infty, y \rightarrow \infty$ Decay: As $x \rightarrow -\infty, y \rightarrow \infty$ As $x \rightarrow \infty, y \rightarrow$ asymptote
RANGE	Increase: $(-\infty, \infty)$ Decrease: $(-\infty, \infty)$	Opens Up: $(y\text{-val}, \infty)$ Opens Down: $(-\infty, y\text{-val})$	Growth: (asymptote, ∞) Decay: $(-\infty, \text{asymptote})$
Interval of INCREASE/DECREASE	Increase: Always $(-\infty, \infty)$ Decrease: Always $(-\infty, \infty)$	Opens Up: INCREASE: $(x\text{-val}, \infty)$ DECREASE: $(-\infty, x\text{-val})$ Opens Down: INCREASE: $(-\infty, x\text{-val})$ DECREASE: $(x\text{-val}, \infty)$	Growth: INCREASE: $(-\infty, \infty)$ DECREASE: $(-\infty, \infty)$

18) Use the following data set to calculate the mean, median, and range.

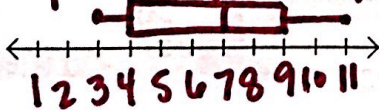
8 12 7 15 19 29 15

Mean: 15 Median: 15 Range: 29 - 7 = 22

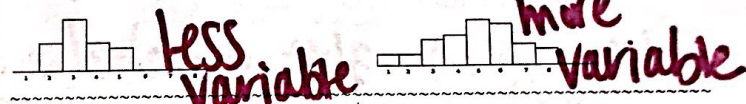
19) Create a box and whisker plot for the following data.

3 3 4 4 4 5 7 8 9 9 9 10 11 11

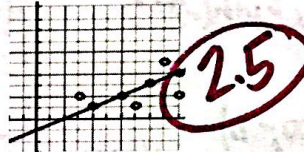
Min: 3 Q1: 4 Median: 7 Q3: 9 Max: 11



20) Label the following histograms as either more or less variable.



21) Based on the graph on the right, what is your y-value when your x-value is 7.5?

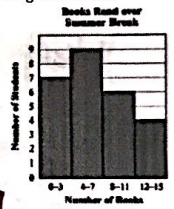


22) Use the histogram to the right to answer the following questions.

How many people total were surveyed?

How many people read 0 - 7 books?

How many people read more than 11 books?



Use the frequency table to answer the following questions.

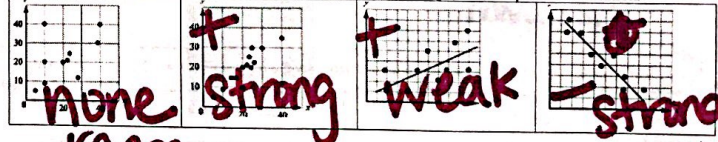
Find the marginal totals for each category.

How many 25-49 year old chose horror?

What percentage of people are 50+ and chose comedy?

	Action	Comedy	Horror	Total
18-25 years old	238	450	312	1,000
25-49 years old	350	472	178	1,000
50+ years old	320	490	190	1,000
Total	908	1,412	680	3,000

23) Label the following graphs as positive, negative, strong, weak, perfect, and/or no correlation.



24) The range of a set of data can be found by subtracting the maximum and the minimum.

25) Data with a strong positive correlation will have a correlation coefficient close to

26) Joint frequencies can be found in the middle of a Two-Way Table.

27) A coefficient is a number which is multiplied by a variable.

28) When using interval notation, open points are indicated by parentheses.