

Unit 1 Study Guide

Name Key S \_\_\_\_\_

Use points  $P(2, -1)$  &  $Q(-9, -6)$  for #1 & 2.

\*1) What coordinate point partitions the directed line segment  $\overline{PQ}$  by a ratio  $\frac{3}{2}$ ?

$$\Delta x \Rightarrow 2 - (-9) = 11 \left(\frac{3}{5}\right) = \frac{33}{5} = 6.6$$

$$\Delta y \Rightarrow -1 - (-6) = 5 \left(\frac{3}{5}\right) = \frac{15}{5} = 3$$

$$x \Rightarrow 2 - 6.6 = -4.6$$

$$y \Rightarrow -1 - 3 = -4$$

$$\boxed{(-4.6, -4)}$$

2) What coordinate point partitions the directed line segment  $\overline{QP}$  by a ratio  $\frac{2}{3}$ ?

$$\Delta x \Rightarrow -9 - 2 = -11 \left(\frac{2}{5}\right) = -\frac{22}{5} = -4.4$$

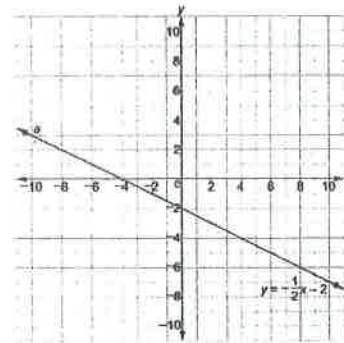
$$\Delta y \Rightarrow -6 - (-1) = -5 \left(\frac{2}{5}\right) = -2$$

$$x \Rightarrow -9 + 4.4 = -4.6$$

$$y \Rightarrow -6 + 2 = -4$$

$$\boxed{(-4.6, -4)}$$

3) An equation of a line  $a$  is  $y = -\frac{1}{2}x - 2$ . See graph.



$$m_1 = -\frac{1}{2}$$

$$m_2 = +2$$

What is the equation of the line that is perpendicular to line  $a$  and passes through point  $(-4, 0)$ .

$$y - y_1 = m_2(x - x_1)$$

$$y - 0 = 2(x - (-4))$$

$$y = 2(x + 4)$$

$$\boxed{y = 2x + 8}$$

Parallelogram  $ABCD$  at right has vertices as shown.

4) What is the perimeter of  $ABCD$ ?

$$\overline{AB} = 2\sqrt{5} = 4.5$$

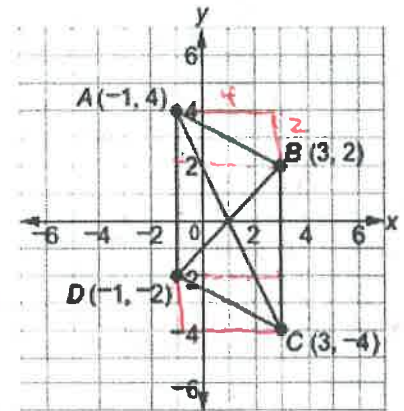
$$2^2 + 4^2 = 4 + 16 = \sqrt{20}$$

$$\overline{BC} = 6$$

$$\overline{CD} = 2\sqrt{5} = 4.5$$

$$\overline{AD} = 6$$

$$\boxed{12 + 4\sqrt{5} \text{ or } 21}$$



5) What is the length of each diagonal?

$$\overline{AC} = \sqrt{(4 - (-4))^2 + (-1 - 3)^2} = \sqrt{8^2 + (-4)^2} = \sqrt{64 + 16} = \sqrt{80}$$

$$\boxed{4\sqrt{5} \text{ or } 8.9}$$

$$\overline{BD} = \sqrt{(2 - (-2))^2 + (3 - (-1))^2} = \sqrt{4^2 + 4^2} = \sqrt{32}$$

$$\boxed{4\sqrt{2} \text{ or } 5.7}$$

6) What is the area of the parallelogram? Area =  $bh$

$$A = bh$$

$$A = (6)(4)$$

$$\boxed{A = 24 \text{ sq unit}}$$

Write the equation of the lines below in slope-intercept form:  $y = mx + b$ .

7) Through  $(-4, 5)$  and parallel to  $y = -\frac{3}{2}x - 5$ .

$$\begin{aligned} (y - y_1) &= m(x - x_1) \\ y - 5 &= -\frac{3}{2}(x - (-4)) \\ y - 5 &= -\frac{3}{2}(x + 4) \\ y - 5 &= -\frac{3}{2}x - 6 \\ y &= -\frac{3}{2}x - 1 \end{aligned}$$

$$\begin{aligned} m_1 &= -\frac{3}{2} \\ m_2 &= -\frac{3}{2} \end{aligned}$$

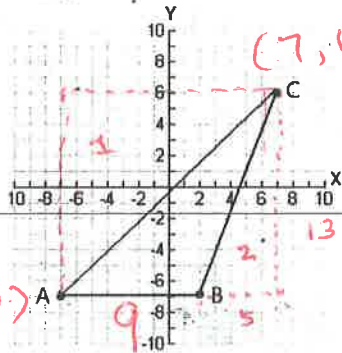
8) Through  $(4, 1)$  and perpendicular to  $y = -2x - 2$

$$\begin{aligned} (y - y_1) &= m(x - x_1) \\ y - 1 &= \frac{1}{2}(x - 4) \\ y - 1 &= \frac{1}{2}x - 2 \\ y &= \frac{1}{2}x - 1 \end{aligned}$$

$$\begin{aligned} m_1 &= -2 \\ m_2 &= \frac{1}{2} \end{aligned}$$

Find the area and perimeter of the following triangle. Simplest form required. Reminder: Draw altitude to find height.

9 Area = 58.5 Perimeter = 42 units



$$\begin{aligned} \text{Altitude} &= 13 \\ A &= 13(9) = 117 \\ A &= 117/2 = 58.5 \end{aligned}$$

$$\begin{aligned} \overline{AB} &= 9 \\ \overline{BC} &= 13.9 \quad 5^2 + 13^2 = c^2 \end{aligned}$$

$$\begin{aligned} \overline{AC} &= \sqrt{(-7-6)^2 + (-7-7)^2} \\ &= \sqrt{(-13)^2 + (-14)^2} \\ &= \sqrt{169 + 196} = \sqrt{365} = 19.1 \end{aligned}$$

$$P = 9 + 13.9 + 19.1 = 42$$

$$A_{\text{rect}} = (14)(13) = 182 \text{ sq units}$$

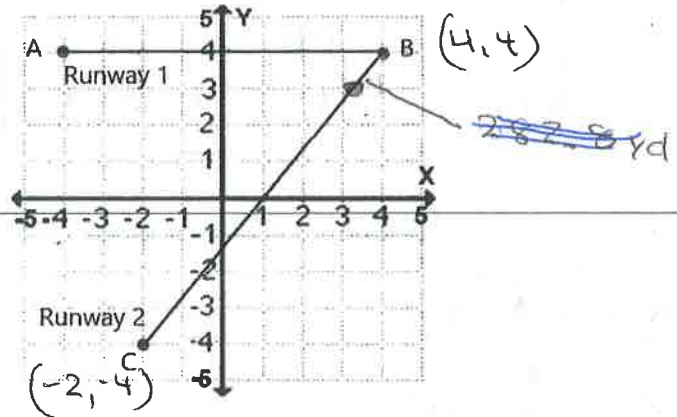
$$A_1 = 182/2 = 91 \text{ sq units}$$

$$A_2 = 5(13) = 65/2 = 32.5 \text{ sq units}$$

$$\text{Area} = 182 - 91 - 32.5 = 58.5 \text{ sq units}$$

In the diagram, two runways intersect at point B. Each square is 200 x 200 yards square. If you walked from A to B and then to C, how far did you walk?

10) 4428 yards



$$\begin{aligned} \overline{AB} &= 8 \text{ units} \times 200 \text{ yd} \\ &= 1600 \text{ yds} \end{aligned}$$

$$\overline{BC} = \sqrt{(4-(-4))^2 + (4-(-2))^2}$$

$$= \sqrt{8^2 + 6^2}$$

$$= \sqrt{64 + 36}$$

$$= \sqrt{100} = 10 \text{ units}$$

$$\text{So, } 10 \times \frac{2828}{200} = \frac{28280}{200} \text{ yd}$$

$$\begin{aligned} \text{Thus, } & 1600 + \frac{28280}{200} = 1600 + 141.4 = 1741.4 \text{ yds} \end{aligned}$$